

## 4.9

### Combining Functions

**Sum, Difference, Product, and Quotient of Functions:** Let  $f$  and  $g$  be two functions with intersecting domains. Then for all values of  $x$  in the intersection, the algebraic combinations of  $f$  and  $g$  are defined by:

**Sum:**  $(f + g)(x) = f(x) + g(x)$

**Difference:**  $(f - g)(x) = f(x) - g(x)$

**Product:**  $(fg)(x) = f(x)g(x)$

**Quotient:**  $\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}$  provided  $g(x) \neq 0$

See Examples 1 – 3 pgs. 140 – 143

See Example 4 pg. 146.

**Composition of Functions:** Let  $f$  and  $g$  be two functions such that the domain of  $f$  intersects the range of  $g$ . The composition of  $g$  denoted  $f \circ g$ , is defined by the rule

$$f \circ g(x) = f(g(x)).$$

The domain of  $f \circ g$  consists of all  $x$ -values in the domain of  $g$  that map to  $g(x)$  values in the domain of  $f$ .

See Examples 5 – 8 pgs. 148-150